

## **WIRELESS COMMUNICATION SYSTEM WITH INTERFERENCE COMPENSATION**

### **Cross reference to related application**

5 A related, co-pending application is U.S. patent application Serial No. \_\_\_, filed concurrently herewith by Foschini et al., and assigned to the assignee hereof, entitled "Wireless Communication System With Interference Compensation".

### **Background of the Invention**

10 This invention relates to wireless communication systems and, more particularly, to wireless communication systems that use techniques that compensate for interference between signals within the system.

15 Signals transmitted between base stations and mobile terminals within a wireless communication system interfere with one another to some extent, thereby negatively affecting the ability of the system to accurately receive and decode these signals. However, various techniques are known to compensate for such interference. These  
20 techniques include compensating for interference by adjusting a signal before it is transmitted to take into account some of the interference the signal will encounter after it is transmitted, and by determining the interference and subtracting this estimated interference from the particular signal after it has been received. Compensating for  
25 interference allows signals to be transmitted within the system at, for example, increased data rates and/or at lower powers, without increasing the error rates, thereby increasing the overall system throughput—the rate of communication traffic the system can handle at any given time.

### **Summary of the Invention**

Among the aforementioned known interference-reduction techniques proposed for both the downlink (base-station-to-mobile-terminal) communication and the uplink (mobile-terminal-to-base-station) communication is so-called dirty paper coding. Another such technique is so-called multi-user detection. Dirty paper coding provides as good and typically better interference reduction on the downlink, but on the uplink dirty paper coding is currently impractical to implement and requires significantly more processing than multi-user detection. The present inventors have thus realized that it is advantageous to use dirty paper coding on the downlink and multi-user detection on uplink. Indeed, wireless communication systems embodying the principles of the invention are configured in just that way.

In particular, using dirty paper coding on downlink signals and multi-user detection on uplink signals, in accordance with the invention, advantageously provides greater interference reduction than if multi-user detection was used on both links, while is being more practical and engendering less processing and at a lower cost than if dirty paper coding was used on both links.

### **Brief Description of the Drawings**

Figure 1 illustrates a portion of a wireless communication system;

Figure 2a illustrates in more detail a cell of the wireless communication system of Figure 1 when multi-user detection is used to compensate for interference among signals within the cell;

Figure 2b illustrates in more detail a cell of the wireless communication system of Figure 1 when multi-user detection is used to compensate for interference among signals within the cell, and where the base station and at least some of the mobile terminals  
5 communicate using multiple antennas;

Figure 3 is a table illustrating for the cell shown in Figure 2a which terminals' signals are taken account of in compensating for interference in which other terminals' signals when multi-user detection is used;

10 Figure 4a illustrates in more detail a cell of the wireless communication system of Figure 1 when dirty paper coding is used to compensate for interference among signals within the cell;

Figure 4b illustrates a plurality of voltage intervals used for explaining a simple version of dirty paper coding;

15 Figure 5 illustrates in more detail a cell of the wireless communication system of Figure 1 when dirty paper coding is used on the downlink and multi-user detection is used on the uplink in accordance with an embodiment of the invention;

20 Figure 6 illustrates in more detail a cell of the wireless communication system of Figure 1 when an order is imposed on the mobile terminals in the cell, pursuant to the principles of the invention, and multi-user detection is used to compensate for interference among signals within the cell;

25 Figure 7 illustrates in more detail a cell of the wireless communication system of Figure 1 when the order is imposed on the mobile terminals in the cell and dirty-paper coding is used to compensate for interference among signals within the cell;

Figure 8 illustrates in more detail a cell of the wireless communication system of Figure 1 when the order is imposed on the

mobile terminals in the cell, pursuant to the principles of the invention, and dirty-paper coding is used on the downlink and multi-user detection is used on the uplink in accordance with an embodiment of the invention;

5 Figure 9 illustrates in more detail a multi-cell portion of the wireless communication system of Figure 1 when the order is imposed on the mobile terminals in the cells, pursuant to the principles of the invention, and dirty-paper coding is used on the downlink and multi-user detection is used on the uplink in accordance with an embodiment of the invention;

10 Figure 10 is a table illustrating for the portion of the system shown in Figure 9 which terminals' signals are taken account of in compensating for interference in which other terminals' signals when the order and multi-user detection are used; and

15 Figure 11 illustrates a wireless communication system similar to that shown in Figure 1 where the order is imposed on the mobile terminals in the entire wireless communication system, pursuant to the principles of the invention, and dirty-paper coding is used on the downlink and multi-user detection is used on the uplink in accordance with an embodiment of the invention.

### **Detailed Description**

Figure 1 illustrates a portion of a wireless communication system 100. The geographic area serviced by system 100 is divided into a plurality of spatially distinct areas called "cells." Although cells 110<sub>1</sub>, ... 100<sub>15</sub> are illustrated as a hexagon in a honeycomb pattern, each cell is actually of an irregular shape that depends on obstacles and topography in the geographical area. Each cell 110<sub>1</sub>, ... 100<sub>15</sub> contains a base station 115<sub>1</sub> ... 115<sub>15</sub>, respectively. Each base station 115<sub>1</sub> ...

115<sub>15</sub> includes equipment to communicate with Mobile Switching Center ("MSC") (not shown), which is connected to local and/or long-distance transmission network, such as a public switch telephone network (PSTN). Each base station 115<sub>1</sub> ... 115<sub>15</sub> also includes radios  
5 and antennas that the base station uses to communicate with mobile terminals.

### Compensation techniques

As described above, signals transmitted between base stations  
10 and mobile terminals within a wireless communication system interfere with one another to some extent, thereby negatively affecting the ability of the system to accurately receive and decode these signals. Various techniques are known to compensate for such interference. Among these techniques are multi-user detection and  
15 dirty paper coding.

Dirty paper coding provides as good or better interference  
reduction on the downlink, but on the uplink dirty paper coding is  
currently impractical to implement and requires significantly more  
processing than multi-user detection. The present inventors have thus  
20 realized that it is advantageous to use dirty paper coding on downlink signals and multi-user detection on uplink signals. In order to explain the operation of a system according to one embodiment of the invention where dirty paper coding is used on the downlink and multi-user detection is used on the uplink, the operation of multi-user  
25 detection and dirty paper coding is now explained. Both multi-user detection and dirty paper coding will first be explained in a one-cell context. After the concept of order, pursuant to the invention, is introduced, both of these compensation techniques will also explained in a multi-cell, and an entire network context. Using these

compensation techniques in the multi-cell or entire network contexts provides the advantage of an even larger throughput improvement than in the one cell context. As described above, this throughput improvement allows the system, for example, to accommodate more  
 5 users.

As is explained in more detail with reference to Figure 2a for the uplink and Figure 2b for the downlink, multi-user detection estimates the interference in a received signal and subtracts this estimated interference from the signal. For further information on the operation and use of multi-user detection see, for example, S. Verdu, MULTI USER  
 10 DETECTION, Cambridge University Press, pp. 154-233, 1998, incorporated herein by this reference.

Figure 2a illustrates cell 110<sub>5</sub> of wireless communication system 100 when multi-user detection is used to compensate for interference among signals within the cell. The cell is represented by 110<sub>5</sub>-M, with  
 15 M used throughout the description and figures to represent that multi-user detection is used.

Cell 110<sub>5</sub>-M includes base station 115<sub>5</sub>-M that communicates with mobile terminals 120<sub>51</sub>-M, 120<sub>52</sub>-M, and 120<sub>53</sub>-M over an uplink and a downlink. The uplink includes communication channels for  
 20 transmitting signals 125<sub>51</sub>, 125<sub>52</sub>, and 125<sub>53</sub>—commonly referred to as uplink signals—from mobile terminals 120<sub>51</sub>-M, 120<sub>52</sub>-M, and 120<sub>53</sub>-M, respectively, to base station 115<sub>5</sub>-M. The downlink includes communication channels for transmitting signals 130<sub>51</sub>, 130<sub>52</sub>, and  
 25 130<sub>53</sub>—commonly referred to as downlink signals—from base station 115<sub>5</sub>-M to mobile terminals 120<sub>51</sub>-M, 120<sub>52</sub>-M, and 120<sub>53</sub>-M, respectively. Multi-user detection can be used on either the uplink, or the downlink, or both.

As can be seen in Figure 2a, base station 115<sub>5</sub>-M receives a received signal that includes all three uplink signals 125<sub>51</sub>, 125<sub>52</sub>, and 125<sub>53</sub>. Because these signals scatter off of objects in the environment and because they have a wide angle of propagation, typically  
5 somewhere between 60° and 360°, these signals interfere with one another, thereby negatively affecting the ability of base station 115<sub>5</sub>-M to use the received signal to accurately decode uplink signals 125<sub>51</sub>, 125<sub>52</sub>, and 125<sub>53</sub>. Multi-user detection can be used to compensate for some of such interference. To use multi-user detection the base station should decode these received signals in an order. The base station then can either 1) determine the theoretical highest system throughput when multi-user detection uses this order, as in the prior art, and assign the data rates and/or power levels based on this calculation or 2) as described in co-pending U.S. patent application  
10 Serial No. \_\_\_, filed concurrently herewith by Foschini et al., and assigned to the assignee hereof, entitled "Wireless Communication System With Interference Compensation", and incorporated herein by this reference, use multi-user detection using this order and determine the data rates and/or power levels assigned to the mobile terminals  
15 based on the requirements of the mobile terminals without regard to the interference introduced by the terminals having a higher index in the order, as described in more detail below.  
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In the illustrative embodiment, the order of the signals is 125<sub>51</sub> first (it will not be interfered with by signals 125<sub>52</sub> and 125<sub>53</sub>), signal  
25 125<sub>52</sub> second (it can be interfered with by signal 125<sub>51</sub>, but it will not be interfered with by signal 125<sub>53</sub>), and signal 125<sub>53</sub> third (it can be interfered with by both 125<sub>51</sub> and 125<sub>52</sub>). Thus, base station 115<sub>5</sub>-M will decode signal 125<sub>53</sub> first, signal 125<sub>52</sub> second, and signal 125<sub>51</sub> third. By transmitting signal 125<sub>53</sub> at a low enough data rate and/or

at a high enough power level, signal 125<sub>53</sub> can be decoded even in the presence of signals 125<sub>51</sub> and 125<sub>52</sub>. Once signal 125<sub>53</sub> is decoded, then the decoded signal is used to reconstruct signal 125<sub>53</sub>. Signal 125<sub>53</sub> is reconstructed into the form in which it was received by base station 115<sub>5</sub>-M. Typically, the signal is reconstructed by first encoding the decoded signal using the coding techniques used to originally encode the signal at the transmitter, and then adjusting this signal to reflect the effect that the channel between the mobile terminal and the base station had on the signal. The latter is accomplished using the channel characteristics of this channel. (Note, the channel characterizations are typically determined by the receiver prior to the start of the data bursts that make up the communications. After receiver determines them it transmits the channel characterization to transmitter. In some cases, for example, so-called time duplexed communication, the transmitter can determine the channel characteristics prior to the start of the data bursts.)

The reconstructed signal is then subtracted from the received signal. This reduces the effect of interference for the remaining signals, i.e. 125<sub>51</sub> and 125<sub>52</sub>, since once signal 125<sub>53</sub> is subtracted it is effectively no longer interference for these other signals. Thus, the next signal to be decoded, signal 125<sub>52</sub> can be sent at a higher data rate and/or a lower power level than if there was no such interference compensation, and still be decoded with an acceptable error rate. This is because when signal 125<sub>53</sub> is subtracted out, the interference from this signal to signal 125<sub>52</sub> is eliminated, or at least substantially reduced. The present inventors have realized that to the extent that mobile terminal 120<sub>53</sub>'s signal is taken account of in mobile terminal 120<sub>52</sub>'s signals, it is as though the former does not exist from the



latter's standpoint and, as such, mobile terminal 120<sub>53</sub> is a "phantom" to mobile terminal 120<sub>52</sub>.

Figure 3 illustrates, for the cell shown in Figure 2a, which mobile terminals' signals are taken account of in compensating for interference in which other mobile terminals' signals, that is, which mobile terminals are phantoms to which other mobile terminals.

Once signal 125<sub>52</sub> is decoded the decoded signal is used to reconstruct signal 125<sub>52</sub> into the form in which it was received by base station 115<sub>5</sub>-M. The reconstructed signal is then subtracted from the received signal. This further reduces the interference for remaining signal 125<sub>51</sub>, since once signals 125<sub>52</sub> and 125<sub>53</sub> are subtracted from the received signal they no longer interfere with signal 125<sub>51</sub>. Thus, signal 125<sub>51</sub> can be sent at higher data rate and/or a lower power level than if there was no such interference compensation, and still be decoded with an acceptable error rate. So, both mobile terminals 120<sub>52</sub>'s and 120<sub>53</sub>'s signals are compensated for in mobile terminal 120<sub>51</sub>'s signal. So, as shown in Figure 3, mobile terminals 120<sub>52</sub> and 120<sub>53</sub> are phantoms to mobile terminal 120<sub>51</sub>.

As can be seen from the description above, multi-user detection can be used on the uplink to allow signals to be transmitted within the system at, for example, increased data rates and/or at lower power levels, without increasing the error rates. This increases the overall system throughput, i.e., the rate of communication traffic the system can handle at any given time.

Furthermore, in addition to being able to transmit a particular signal at higher data rate and/or a lower power level, because the communications between the base stations and mobile terminals are suffering less interference, the reduced interference could allow

additional mobile terminals to be able to communicate with the base station.

However, on the downlink, particularly when the base station and mobile terminals communicate using more than one antenna, multi-user detection is not very effective in increasing the overall system throughput. In particular, similarly to the uplink signals, the downlink signals scatter off of objects in the environment and have a wide angle of propagation. Thus, these signals interfere with one another. Although, a particular mobile terminal may receive many of the downlink signals for communication with other mobile terminals, these signals are typically not received at power levels that allow the particular mobile terminal to detect them and to decode them acceptably enough to be able to subtract them out. Thus, at some mobile terminals multi-user detection can be used to compensate for only a few of the interfering signals that impinge upon it, and at other mobile terminals multi-user detection cannot be used at all on the downlink.

Additionally, when, as shown in Figure 2b, base station 215<sub>5</sub>-M communicates with mobile terminals 220<sub>51</sub>-M, 220<sub>52</sub>-M, and 220<sub>53</sub>-M using multiple antennas, then it is particularly difficult, or even impossible, to detect the signals meant for other mobile terminals. Cell 210<sub>5</sub>-M of Figure 2b is similar to cell 110<sub>5</sub>-M of Figure 2a, except the base station and/or some of the mobile terminals of cell 210<sub>5</sub>-M have multiple transmit and/or receive antennas. Cell 210<sub>5</sub>-M can be used in wireless communication system 100 instead of cell 110<sub>5</sub>-M. Cell 210<sub>5</sub>-M includes base station 215<sub>5</sub>-M, which has two transmit/receive antennas 270<sub>51</sub> and 270<sub>52</sub>; mobile terminals 220<sub>51</sub>-M and 220<sub>53</sub>-M, which have two transmit/receive antennas 275<sub>51</sub> and 275<sub>52</sub>, and 275<sub>54</sub> and 270<sub>55</sub>, respectively; and mobile terminal 220<sub>52</sub>,

which has one transmit/receive antenna 275<sub>53</sub>. Each of the base station antennas 270<sub>51</sub> and 270<sub>52</sub> transmits a downlink signal to each of the mobile terminals. Thus, antennas 270<sub>51</sub> and 270<sub>52</sub> transmit signals 230<sub>51</sub> and 230<sub>52</sub> to mobile terminal 220<sub>51</sub>-M, signals 230<sub>53</sub> and 230<sub>54</sub> to mobile terminal 220<sub>52</sub>-M, and signals 230<sub>55</sub> and 230<sub>56</sub> to mobile terminal 220<sub>53</sub>-M. Each of the signals transmitted to a particular mobile terminal is received by each of its antennas. Additionally, some, or even all of the signals transmitted to the other mobile terminals are received by each of the particular mobile terminal's antennas. For example, signals 230<sub>55</sub> and 230<sub>56</sub>, transmitted to mobile terminal 220<sub>53</sub>-M, are transmitted at a power level and rate that will allow this mobile terminal to detect the signals considering the channel characteristics between the transmit and receive antennas (270<sub>51</sub> and 270<sub>52</sub>, and 275<sub>55</sub> and 275<sub>56</sub>, respectively) and the number of antennas at the transmitter (in this case base station 215<sub>5</sub>-M) and the receiver (in this case mobile terminal 220<sub>53</sub>-M). However, the signals transmitted to the other mobile terminals are transmitted at a power level and data rate that will allow those other mobile terminals to detect them, but not necessarily for mobile terminal 220<sub>53</sub>-M to detect them. Due to the fact that the channel characteristics and interference are used to determine power levels/data rates for one set of antennas to be able to receive a signal, and the fact that the channel characteristics and interference are different for different sets of antenna, it is often unlikely that a signal that is sent at a power level/data rate that will allow it to be received by one set of antennas at one mobile terminal will also allow it to be received at an acceptable power level/data rate to decode at a different set of antennas that are at a different mobile terminal. Thus, it is highly unlikely that mobile terminal 220<sub>53</sub>-M will be able to detect

signals  $230_{51}$ ,  $230_{52}$ , or  $230_{53}$  that are transmitted to other mobile terminals. Thus, mobile terminal  $220_{53}$ -M will not be able to subtract out these signals, and so multi-user detection cannot be effectively used on the downlink to mobile terminal  $220_{53}$ -M. Similarly, multi-user detection cannot be used on the downlink to mobile terminals  $220_{51}$ -M and  $220_{52}$ -M.

It is thus seen, as indicated earlier, that multi-user detection is quite effective on the uplink in increasing the overall system throughput, while on the downlink multi-user detection is less effective in doing so.

As described above, dirty paper coding often provides better interference reduction on the downlink. As is explained in more detail with reference to Figure 4a, dirty paper coding compensates for interference by adjusting a signal, before it is transmitted, to take into account some of the interference the signal will encounter after it is transmitted. For further information on the operation and use of dirty paper coding see, for example, M. Costa, "Writing on Dirty paper", IEEE Transactions on Information Theory, Vol. 29, No. 3, pp. 439, 1983 (Appendix A); and U. Erez, S. Shamai, R. Zamir, "Capacity and Lattice-Strategies for Canceling Known Interference", ISIS, Honolulu Hawaii, USA, Nov 5-8, 2000, both incorporated herein by this reference.

Figure 4a illustrates in more detail cell  $110_5$  of wireless communication system 100 when dirty paper coding is used to compensate for interference among signals within the cell. The cell is represented by  $110_5$ -D, with D used throughout the description and figures to represent that dirty paper coding is used. Similarly to cell  $110_5$ -M, cell  $110_5$ -D includes base station  $115_5$ -D that communicates with mobile terminals  $120_{51}$ -D,  $120_{52}$ -D, and  $120_{53}$ -D via uplink

signals 145<sub>51</sub>, 145<sub>52</sub>, and 145<sub>53</sub> and downlink signals 150<sub>51</sub>, 150<sub>52</sub>, and 150<sub>53</sub>.

On the downlink, each mobile terminal 120<sub>51</sub>-D, 120<sub>52</sub>-D, and 120<sub>53</sub>-D receives all of the downlink signals 150<sub>51</sub>, 150<sub>52</sub>, and 150<sub>53</sub> transmitted by base station 115<sub>5</sub>-D and needs to decode the particular signal directed to it. These signals interfere with one another, thereby negatively affecting the ability of the mobile terminals to accurately decode the signal directed to the mobile terminals. Dirty paper coding can be used to compensate for some of such interference. To use dirty paper coding, base station 115<sub>5</sub>-D should impose some sort of order on the mobile terminals before it transmits the signals to the terminal. The order determines who is being interfered with by whom. The base station then can either 1) determine the theoretical highest system throughput when dirty-paper coding uses this order, as in the prior art, and assign data rates and/or power covariance matrices based on this calculation, or 2) as described in co-pending U.S. patent application Serial No. \_\_\_, filed concurrently herewith by Foschini et al., and assigned to the assignee hereof, entitled "Wireless Communication System With Interference Compensation", use dirty paper coding using this order and determine the data rates and/or power levels assigned to the mobile terminals based on the requirements of the mobile terminals without regard to the interference introduced by the terminals having a higher index in the order, as described in more detail below.

In the illustrative embodiment, the order imposed is mobile terminal 120<sub>51</sub> first, mobile terminal 120<sub>52</sub> second, and mobile terminal 120<sub>53</sub> third. Mobile terminals 120<sub>51</sub> will suffer no interference from 120<sub>52</sub> and 120<sub>53</sub>. Mobile terminal 120<sub>52</sub> will suffer no inference from 120<sub>53</sub> and can suffer interference from 120<sub>51</sub>. Mobile terminal

120<sub>53</sub> can suffer interference from both 120<sub>51</sub> and 120<sub>52</sub>. Signals 150<sub>51</sub>, 150<sub>52</sub>, and 150<sub>53</sub> are typically multi-dimensional. A simple explanation of dirty paper coding with one dimensional symbols is now provided with reference to Figures 4a and 4b, one skilled in the art can use this explanation and the reference cited above to implement dirty paper coding with multi-dimensional symbols. (Note, the signals are typically multi-dimensional due to the time coding of these signals prior to transmission and to the plurality of antennas used to transmit and/or receive them). At a particular time the mobile terminal whose interference is being compensated for (removed) is used, as described below, to adjust the signal from the mobile terminal being interfered with. If there is more than one mobile terminal whose interference is being compensated for, then the signals of the mobile terminal with the last index order (in this case three) is used to adjust the signal of the mobile terminal with the second to last index order (in this case two). This adjusted signal is then used to adjust the signal of the mobile terminal with the third to last index order, and so on until the signal of the mobile terminal with order of one is so adjusted.

The way the signals are transmitted is now first explained without the use dirty paper coding, and then with its use. At a particular time each signal is transmitted using a voltage within a voltage interval. The voltage intervals are ranges of voltages, some of which are shown in Figure 4b. The voltage intervals are different for the different mobile terminals. For example, the voltage intervals for 150<sub>52</sub> are 10 V apart, such as -5V to 5V, 5V to 15V, 15 to 25, etc, and for 150<sub>51</sub> are 2 V apart, such as -1V to 1V, 1V to 3V, 3 to 5, etc. Each of the voltage intervals includes a discrete number of voltages, each of which is mapped to a particular binary number. The discrete voltages in same location within each of the voltage intervals for the same

mobile terminal correspond to the same binary number. For example, for the 10 V intervals (voltage intervals<sub>2</sub>) -6.8V, 3.2V, and 13.2V are all mapped to the same binary number. For the 2V intervals (voltage intervals<sub>1</sub>) -3.2V, -1.2V, .8V, 2.8V, 4.8V, 6.8V, 8.8V, 10.8V, 12.8V, 14.8V, and 16.8 are all mapped to the same binary number. If  $150_{51}$  is .8,  $150_{52}$  is 3.2V, and  $150_{53}$  is 11.4V, then without the use of dirty paper, base station 115<sub>5</sub>-D would transmit a transmit signal that included each of signals  $150_{51}$ ,  $150_{52}$ , and  $150_{53}$ , typically with each signal at a different data rate or power level, and these signals would interfere with each other.

With the use of dirty paper coding the transmit signal is obtained in the following way. First signal  $150_{52}$  is compensated for the interference of signal  $150_{53}$ .  $\text{Int}_1$  shows the amount of interference provided by signal  $150_{53}$ , in order to eliminate this interference for signal  $150_{52}$ , yet not completely eliminate signal  $150_{53}$ , determine using the intervals related to  $150_{52}$ , i.e. voltage intervals<sub>2</sub>, the closest discrete voltage to the voltage of signal  $150_{53}$ , i.e. 11.4V that corresponds to the same binary number as the voltage of signal  $150_{52}$ , i.e. 3.2V. In this case the closest binary voltages to 11.4V that correspond to the same binary number as 3.2V are 3.2V and 13.2V. 13.2V is closer to 11.4V than 3.2V is to 11.4V. Thus, 13.2V represents the compensated signal  $150_{52}$ , that is, signal  $150_{52}$  compensated for signal  $150_{53}$ .

If the only two signals in cell 110<sub>5</sub>-D were  $150_{52}$  and  $150_{53}$  then 13.2V could be transmitted and both mobile terminals 120<sub>52</sub>-D and 120<sub>53</sub>-D would be able to decode their signals.

Compensated signal  $150_{52}$  is then used to compensate signal  $150_{51}$ .  $\text{Int}_2$  shows the amount of interference provided by compensated signal  $150_{52}$ , in order to eliminate this interference for

signal  $150_{51}$ , yet not completely eliminate signal  $150_{52}$ , determine the closest discrete voltage (using the intervals related to  $150_{51}$ , that is voltage intervals<sub>1</sub>) to the voltage of compensated signal  $150_{52}$ , i.e. 13.2V that corresponds to the same binary number as the voltage of signal  $150_{51}$ , i.e. .8V. In this case the closest binary voltages to 13.2V that correspond to the same binary number as .8V are 14.8V and 12.8V. 12.8V is closer to 13.2V than 14.8V is to 13.2V. Thus, 12.8V represents the compensated signal  $150_{51}$ , that is, signal  $150_{51}$  compensated for signals  $150_{52}$  and  $150_{53}$ . Therefore, 12.8V is the transmitted signal.

Thus, mobile terminal  $120_{53}$ 's signals are taken account of in mobile terminal  $120_{52}$ 's signal, so mobile terminal  $120_{53}$  is a phantom to mobile terminal  $120_{52}$ . And both mobile terminals  $120_{52}$ 's and  $120_{53}$ 's signals are taken account of in mobile terminal  $120_{51}$ 's signals, so mobile terminals  $120_{52}$  and  $120_{53}$  are phantoms to mobile terminal  $120_{51}$ .

In the multi-dimensional symbol context the voltages transmitted are actually voltage vectors, the interference voltage is a vector, and the voltage interval is a voltage lattice component.

Although, the prior art discusses dirty paper coding, the present inventors are not aware of the art discussing using dirty paper coding on the uplink, nor of what is to be used on the uplink when dirty paper coding is used on the downlink. In order to use dirty paper coding on the uplink the signals from all of mobile terminals  $120_{51}$ -D,  $120_{52}$ -D, and  $120_{53}$ -D have to be somehow passed to one transmitter that would transmit them to the base station. This is quite difficult to implement. Indeed it is currently impractical. Furthermore, even if it was implementable, as the present inventors have realized as can be seen from our above explanations of dirty paper, dirty paper coding is more



computationally burdensome, and thus requires more processing power, than multi-user detection.

As described above, dirty paper coding provides a better interference reduction on the downlink than multi-user detection.

5 However, as also described above, dirty paper coding is not currently practical on the uplink. The present inventors have thus realized that it is advantageous to use dirty paper coding on downlink signals and multi-user detection on uplink signals.

10 Figure 5 illustrates in more detail cell 110<sub>5</sub> of wireless communication system 100 when dirty paper coding is used on the downlink and multi-user detection is used on the uplink. The cell is represented by 110<sub>5</sub>-DM, with DM used throughout the description and figures to represent that dirty paper coding is used on the downlink and multi-user detection is used on the uplink.

15 Similarly to cells 110<sub>5</sub>-M and 110<sub>5</sub>-D, cell 110<sub>5</sub>-DM includes base station 115<sub>5</sub>-DM that communicates with mobile terminals 120<sub>51</sub>-DM, 120<sub>52</sub>-DM, and 120<sub>53</sub>-DM via uplink signals 125<sub>51</sub>, 125<sub>52</sub>, and 125<sub>53</sub> and downlink signals 150<sub>51</sub>, 150<sub>52</sub>, and 150<sub>53</sub>. In this scenario the uplink operates as described above with reference to the uplink for multi-user detection and the downlink operates as described above  
20 with reference to the downlink for dirty paper coding.

Using dirty paper coding on downlink signals and multi-user detection on uplink signals, in accordance with the invention, advantageously provides greater interference reduction than if multi-user detection was used on both links, while is easier to implement  
25 and engendering less processing than if dirty paper coding was used on both links.

Additionally, as the present inventors have realized, that it is desirable to compensate particular terminals' signals for interference

from other terminal's signals, and thus allow some mobile terminals to be phantoms to other mobile terminal. Particularly, the present inventors have realized that it would be desirable to have a system that provides a readily implementable system where on both links mobile terminals are phantoms to each other, referred to herein as a "phantom net" system. As described above, the present inventors have also realized that such a phantom net system can be achieved on the uplink and the downlink on a predictable basis by using multi-user detection on the uplink and dirty paper coding on the downlink. Therefore, the present invention provides an implementable system where on both links mobile terminals are phantoms to each other. Furthermore, in accordance with co-pending U.S. patent application Serial No. \_\_, \_\_ filed concurrently herewith by Foschini et al., and assigned to the assignee hereof, entitled "Wireless Communication System With Interference Compensation", at least one mobile terminal will be compensated for the interference from all other mobile terminals on the uplink. Similarly, at least one mobile terminal, not necessarily the same one as on the downlink, will be so compensated on the downlink. Thus, all of the mobile terminals (except the terminal that has an index of one) in a particular portion of wireless system 100 will be phantoms to at least one mobile terminal.

#### Operating Parameter Assignment.

As discussed above, a problem arises because of the way in which in the disclosures of dirty paper coding and multi-user detection (which are largely theoretical in nature) assign the data rate (or set of data rates) and/or power covariance matrices to each mobile terminal. Typically, data rate and/or power covariance matrices is assigned based on the theoretical highest system throughput that can be

achieved using the particular compensation technique at a particular instant in time given the conditions that then exist. (The theoretical highest system throughput refers to the maxim theoretically obtainable throughput for the system or for the portion of the system being considered and not to the throughput of the individual mobile terminals.) The conditions are typically, e.g., the number of terminals and their channel characteristics, the uplink and downlink transmit power levels, etc. There may also be discussions assigning data rate and/or power covariance matrices based on weighted theoretical highest system capacity, which determines the theoretical highest system capacity when certain mobile terminals' rates are weighted. The weighting can be, for example, the revenue per bit per second associated with the mobile terminal. Some of the theoretical calculations are described in, for example, S. Verdu, MULTI USER DETECTION, (cited above) for multi-user detection; and in for example M. Costa, "Writing on Dirty paper", (cited above), U. Erez, S. Shamai, R. Zamir, "Capacity and Lattice-Strategies for Canceling Known Interference" (cited above), and S. Vishwanath, N. Jindal, and A. Goldsmith "On the Capacity of Multiuple Input Multiple Output Broadcast Channels" Department of Electrical Engineering, Stanford University, Stanford, CA 94305 <http://wsl.stanford.edu/> for dirty paper coding.

The present inventors have realized that it is advantageous to assign an operating parameter, such as the data rate, the power level, the power covariance matrix, or the set of data rates, to the mobile terminals without determining the maximal system throughput, and without determining the maximal weighted system throughput. This can be accomplished by imposing an order on the terminals and assigning the operating parameter such that at least one of operating

parameter values of terminals that have a lower index in the order will not be made worse due to the presence of terminals having a higher index in the order. (Making an operating parameter value worse means reducing the efficacy of the communication, for example, for data rate  
 5 reduced efficacy means a reduced data rate, and for power level reduced efficacy means an increased power level.) The operating parameter values are assigned to the terminals in the order.

The above means that the data rate and/or power covariance matrices are assigned such that the data rates of the terminals having  
 10 a lower index in the order will not be decreased due to the presence of the terminals having a higher index in the order, and this is accomplished without changing the power covariance matrices of the antennas involved in the communication with the lower indexed terminals. (Note a mobile terminals index in the order is its order  
 15 number, so a mobile terminal that is first in the order has the lowest order index, of one; and a mobile terminal that is second in the order has an index of two, and thus has a higher index in the order than the mobile terminal whose index is one.) The compensation scheme (such  
 20 as dirty paper coding or multi-user detection) is used to compensate for interference among the signals. The compensation performed using an order of the terminals that defines which terminals' signals are used to compensate for interference in which other terminals' signals. So, the assignment is made to the terminals based on the terminals requirements without regard to the interference introduced  
 25 by the terminals lower in the order since this interference will be compensated for by the compensation technique when the compensation technique process the terminals in accordance with the order. Assigning the data rate and/or power level to the mobile terminals without determining the maximal system throughput, and

without determining the maximal weighted system throughput is in marked contrast to the prior art approach in which at least one of the above is maximized through complex calculations. Thus, the invention reduces the amount of computation necessary to implement such techniques on an ongoing, real-time basis in a real-world system.

Figure 6 illustrates in more detail cell 210<sub>5</sub> when the order is imposed on the mobile terminals in the cell, pursuant to the principles of the invention, and multi-user detection is used to compensate for interference among signals within the cell. The cell shown in Figure 6 being represented by 210<sub>5</sub>-M<sub>S</sub>, with M<sub>S</sub> used throughout the description and figures to represent that multi-user detection with order is used.

As described above, with reference to Figure 2a, cell 110<sub>5</sub>-M can operate 1) using the assignment of data rates/power levels based on the highest obtainable system throughput for this particular system when multi-user detection uses this order or 2) using multi-user detection that uses this order and determining the data rates and/or power levels assigned to the mobile terminals based on the requirements of the mobile terminals without regard to the interference introduced by the terminals having a higher index in the order, and without the determination of the highest system throughput, in accordance with co-pending U.S. patent application Serial No. \_\_, \_\_ filed concurrently herewith by Foschini et al., and assigned to the assignee hereof, entitled "Wireless Communication System With Interference Compensation". Cell 210<sub>5</sub>-M<sub>S</sub>, shown in Figure 6, is the version of cell 110<sub>5</sub>-M that does not determine the highest system throughput and in which the base station and/or some of the mobile terminals have multiple transmit and/or receive

antennas. Cell 210<sub>5</sub>-M can be used in wireless communication system 100 instead of cell 110<sub>5</sub>.

In one embodiment of the invention, the order used in cell 210<sub>5</sub>-M<sub>S</sub> is determined by processor 560<sub>5</sub>-M of base station 115<sub>5</sub>-M<sub>S</sub>. In other embodiments of the invention the order can be determined at any processor, controller, or other equipment within wireless system 100, such as for example the Mobile Switching Center (MSC). The order can then be passed to base station 115<sub>5</sub>-M<sub>S</sub>.

The order can be determined randomly or, alternatively, the order can be based on some predefined criterion or criteria that may prove advantageous in using as much system capacity as possible without actually having to calculate the theoretically highest system throughput. For example, the order can be based on the order in which the mobile terminals initiated a communication session with the base station(s) (either ascending or descending); the order might be based on the amount of data to be transmitted to or from the various mobile terminals; or the order might be based on which mobile terminal could make best use of the communication resources on an individual basis (as opposed to the overall basis used in the prior art calculations). Maximizing a performance criteria can be, for example, by determining which mobile terminal achieves a required rate with least power when the determination is made for each mobile terminal assuming an absence of the other mobile terminals in the system. The mobile terminal that achieves this required rate with the least power is given the index in the order of one. This is then repeated for the remaining mobile terminals, except the assumption now is that they are interfered with by mobile terminals that have already been assigned an index in the order but not interfered by the mobile terminals that have not been assigned an index. The last step is

repeated until all of the mobile terminals are assigned an order. Alternatively, maximizing a performance criteria can be, for example, achieving a maximum rate at specified power level per user.

In the illustrative embodiment, for example, the order is based on the order in which mobile terminals initiated a communication session with the base station. If mobile terminal  $220_{51}$  initiated a communication session with base station  $215_5-M_S$  first, mobile terminal  $220_{52}$  second, and mobile terminal  $220_{53}$  third, then the order of the mobile terminals is  $220_{51}$  first,  $220_{52}$  second, and  $220_{53}$  third. So, base station  $215_5-M$  will decode signals  $225_{54}$  and  $225_{55}$  first, signal  $225_{53}$  second, and signals  $225_{51}$   $225_{52}$  third. This order means that on the uplink mobile terminals  $220_{52}$  and  $220_{53}$  are phantoms to mobile terminal  $220_{51}$ , and mobile terminal  $220_{53}$  is a phantom to mobile terminal  $220_{52}$ . Note, that the signals from the same mobile terminal, even when there are several signals from the same mobile terminal, count as only one element in the scheme of the order, there can be exceptions when the signal are carrying files that have different performance needs.

Because mobile terminals  $220_{52}$  and  $220_{53}$  are phantoms to mobile terminal  $220_{51}$ , the signals of mobile terminals  $220_{52}$  and  $220_{53}$  do not interfere with the signals of mobile terminal  $220_{51}$ , so the signals to mobile terminal  $220_{51}$  can be assigned a data rate and a power level based on its requirements without consideration of the signal to mobile terminals  $220_{52}$  and  $220_{53}$  and without consideration of the highest obtainable system throughput. So, for example, if mobile terminal  $220_{51}$  is constrained to a certain power level, then mobile terminal  $220_{51}$  gets the highest data rate that can be supported at this power level considering that the signals to mobile terminal  $220_{51}$  are not interfered with by the signals to mobile terminals  $220_{52}$

and 220<sub>53</sub>. This highest data rate can be determined using well-known techniques such as water pouring. Water pouring selects the power allotments used at the virtual antenna at various frequencies, for further information on water pouring see for example, J. J. Raleigh, and J. M. Cioffi "Spacial-Temporal Coding for Wireless Communication" IEEE Transaction on Communications, Vo. 46 March 1998, p. 357, R.R. Farrokhi, G.J, Foschini, R.A. Valenzuela "Link-Optimal Space-Time Processing with Multiple Transmit and Receive Antennas" IEEE Communications Letters, Vol. 5, No. 3 March 2001, p. 85, both incorporated herein by this reference.

And, if mobile terminal 220<sub>51</sub> requires certain a data rate, then mobile terminal 220<sub>51</sub> gets the lowest power level needed to support this power level considering that the signals to mobile terminal 220<sub>51</sub> are not interfered with by the signals to mobile terminals 220<sub>52</sub> and 220<sub>53</sub>. This lowest power level can be determined using well-known techniques such as water pouring.

Similarly because mobile terminal 220<sub>53</sub> is a phantom to mobile terminal 220<sub>52</sub>, mobile terminal 220<sub>52</sub> can be assigned a data rate and/or power level based on its requirements without consideration of the signal to mobile terminal 220<sub>53</sub> and without consideration of the highest obtainable system throughput.

On the uplink, cell 210<sub>5</sub>-M<sub>s</sub> operates similarly to cell 210<sub>5</sub>-M, described above with reference to Figure 2a, except to detect the signals the base station has to use techniques used to detect signals in multiple antenna environments. Such techniques are, for example, water pouring in the presence of interference, discussed in, for example, the J. J. Raleigh, and J. M. Cioffi "Spacial-Temporal Coding for Wireless Communication" reference, and the R.R. Farrokhi, G.J,



Foschini, R.A. Valenzuela "Link-Optimal Space-Time Processing with Multiple Transmit and Receive Antennas" reference.

Thus, the data rate and/or power level is assigned to the mobile terminals without determining the maximal system throughput, and without determining the maximal weighted system throughput. Additionally, the data rate and/or power level are assigned such that the data rates of the terminals having a lower index in the order will not be decreased due to the presence of the terminals having a higher index in the order, and this is accomplished without changing the power covariance matrixes of the antennas involved in the communication with the lower indexed terminals.

Although, the order can be imposed on the uplink, the downlink, or both, when multi-user detection is used on both the uplink and the downlink, it may be beneficial to impose the order on just the uplink. It may not be beneficial to impose the order on the downlink when multi-user detection is used on the downlink, since, as described above, on the downlink each mobile terminal may not be able to decode the downlink signals for communication with other mobile terminals. Thus, the mobile terminal may not be able to decode the signals in the order. Furthermore, because of the power level with which a particular mobile terminal receives all of the downlink signals it may be easier to decode them in an order different from the aforementioned order. Thus, it may or may not be beneficial to impose the order on the downlink when multi-user detection is used.

Figure 7 illustrates in more detail cell 210<sub>5</sub> when the order is imposed on the mobile terminals in the cell, pursuant to the principles of the invention, and dirty-paper coding is used to compensate for interference among signals within the cell. The cell is represented by

210<sub>5</sub>-Ds, with D<sub>s</sub> used throughout the description and figures to represent that dirty paper coding with order is used.

As described above with reference to Figure 4a, cell 110<sub>5</sub>-D can operate 1) using the assignment of data rates/power levels based on the highest obtainable system throughput for this particular system when multi-user detection uses this order, or 2) using multi-user detection that uses this order and determining the data rates and/or power levels assigned to the mobile terminals based on the requirements of the mobile terminals without regard to the interference introduced by the terminals having a lower index the order, and without the determination of the highest system throughput, in accordance with co-pending U.S. patent application Serial No. \_\_, \_\_ filed concurrently herewith by Foschini et al., and assigned to the assignee hereof, entitled "Wireless Communication System With Interference Compensation". Cell 210<sub>5</sub>-Ds, shown in Figure 7, is the version of cell 110<sub>5</sub>-D that does not determine the highest system throughput and in which the base station and/or some of the mobile terminals of cell 210<sub>5</sub> have multiple transmit and/or receive antennas. Cell 210<sub>5</sub>-M can be used in wireless communication system 100 instead of cell 110<sub>5</sub>.

Similarly to the above described embodiment where order is used with multi-user detection, shown in Figure 6, the order can be determined by processor 560<sub>5</sub>-D, or it can be determined by any processor or other equipment within wireless system 100 and then passed to base station 115<sub>5</sub>-Ds. As described above, the order can be determined randomly or, alternatively, the order can be based on some predefined criterion or criteria that may prove advantageous in using as much system throughput as possible, as described above.

In the illustrative embodiment, for example, the order is based on the amount of data to be transmitted to the various mobile terminals, with smallest amount of data being first and the largest being last. If at a particular time mobile terminal 220<sub>51</sub> has the smallest amount of data, mobile terminal 220<sub>52</sub> has the next smallest, and mobile terminal 220<sub>53</sub> has the largest, then the order of the mobile terminals is 220<sub>51</sub> first, 220<sub>52</sub> second, and 220<sub>53</sub> third. So, base station 215<sub>5</sub>-M will process signals 225<sub>55</sub> and 225<sub>56</sub> first, signals 225<sub>53</sub> and 225<sub>54</sub> second, and signals 225<sub>51</sub> and 225<sub>52</sub> third. This order means that on the downlink mobile terminals 220<sub>52</sub> and 220<sub>53</sub> are phantoms to mobile terminal 220<sub>51</sub>, and mobile terminal 220<sub>53</sub> is a phantom to mobile terminal 220<sub>52</sub>.

Because mobile terminals 220<sub>52</sub> and 220<sub>53</sub> are phantoms to mobile terminal 220<sub>51</sub>, the signals of mobile terminals 220<sub>52</sub> and 220<sub>53</sub> do not interfere with the signals of mobile terminal 220<sub>51</sub> then the signal to mobile terminal 220<sub>51</sub> can be assigned a data rate and a power level based on its requirements without consideration of the signal to mobile terminals 220<sub>52</sub> and 220<sub>53</sub> and without consideration of the highest obtainable system throughput. So, as described above if mobile terminal 220<sub>51</sub> is constrained to a certain power level or certain data rate, then mobile terminal 220<sub>51</sub>'s other criteria can be determined using the consideration that the signals to mobile terminal 220<sub>51</sub> are not interfered with by the signals to mobile terminals 220<sub>52</sub> and 220<sub>53</sub>. The data rate or power level can be determined using well-known techniques such as water pouring, described in the J. J. Raleigh, and J. M. Cioffi "Spatial-Temporal Coding for Wireless Communication" reference, and the R.R. Farrokhi, G.J. Foschini, R.A. Valenzuela "Link-Optimal Space-Time Processing with Multiple Transmit and Receive Antennas" reference.

Similarly because mobile terminal 220<sub>53</sub> is a phantom to mobile terminal 220<sub>52</sub>, mobile terminal 220<sub>52</sub> can be assigned a data rate and a power level based on its requirements without consideration of the signal to mobile terminal 220<sub>53</sub> and without consideration of the highest obtainable system throughput.

Thus, the data rate and/or power level is assigned to the mobile terminals without determining the maximal system throughput, and without determining the maximal the weighted system throughput. Additionally, the data rate and/or power level are assigned such that the data rates of the terminals having a lower index in the order will not be decreased due to the presence of the terminals having a higher index in the order, and power levels of the terminals having a lower index in the order will not be increased due to the presence of the terminals having a higher index in the order.

On the downlink cell 210<sub>5</sub>-D<sub>S</sub> operates as described above with reference to Figure 4a, except to detect the signals the base station has to use techniques used to detect signals in multiple antenna environments. This can be accomplished as described above using water pouring. Note that the signals to the same mobile terminal, even when there are several signals to the same mobile terminal, count as only one element in the scheme of the order, there can be exceptions when the signal are carrying files that have different performance needs.

As described above, currently, it is impractical to use dirty paper coding on the uplink. However, if it were possible dirty paper coding is used on the uplink, the order can be imposed on the uplink in addition to or instead of on the downlink.

As described above, both 1) assigning the data rate and/or power levels to the mobile terminals based on the requirements of the mobile

terminals without regard to the interference introduced by the terminals having a higher index the order, and without the determination of the highest system throughput, in accordance with co-pending U.S. patent application Serial No. \_\_, \_\_ filed concurrently herewith by Foschini et al., and assigned to the assignee hereof, entitled "Wireless Communication System With Interference Compensation", and 2) using dirty paper coding on the downlink and multi-user detection improves the overall performance of the wireless communication system. In the preferred embodiment of the invention, the two are used together, as shown in Figure 8.

Figure 8 illustrates in more detail cell 210<sub>5</sub> when the order is imposed on the mobile terminals in the cell, pursuant to the principles of the invention, and dirty paper coding is used on the downlink and multi-user detection is used on the uplink. The cell is represented by 210<sub>5</sub>-DM<sub>s</sub>, with DM<sub>s</sub> used throughout the description and figures to represent that dirty paper coding with order is used on the downlink and multi-user detection with order is used on the uplink.

As described above with reference to Figure 5, cell 110<sub>5</sub>-DM can operate 1) using the assignment of data rates/power levels based on the highest obtainable system throughput for this particular system when multi-user detection uses this order, or 2) using multi-user detection that uses this order and determine the data rates and/or power levels assigned to the mobile terminals based on the requirements of the mobile terminals without regard to the interference introduced by the terminals having a higher index the order, and without the determination of the highest system throughput, in accordance with co-pending U.S. patent application Serial No. \_\_, \_\_ filed concurrently herewith by Foschini et al., and assigned to the assignee hereof, entitled "Wireless Communication

System With Interference Compensation". Cell 210<sub>5</sub>-DM<sub>S</sub>, shown in Figure 8, is the version of cell 110<sub>5</sub>-DM that does not determine the highest system throughput and in which the base station and/or some of the mobile terminals of cell 210<sub>5</sub> have multiple transmit and/or receive antennas. Cell 210<sub>5</sub>-M can be used in wireless communication system 100 instead of cell 110<sub>5</sub>.

Similarly to the above described embodiments, the order can be determined by processor 560<sub>5</sub>-DM, or it can be determined by any processor or other equipment within wireless system 100 and then passed to base station 215<sub>5</sub>-DM<sub>S</sub>. As described above the order can be determined randomly or, alternatively, the order can be based on some predefined criterion or criteria that may prove advantageous in using as much system throughput as possible, as described above. In the illustrative embodiment of cell 210<sub>5</sub>-DM<sub>S</sub> order is imposed for both the downlink and the uplink.

When order is used on both links either 1) the same criteria can be used to determine the order on both downlink and uplink communications, or, alternatively, 2) different criteria can be used for downlink and uplink communication. For example, on the uplink the order can be based on the order in which the mobile terminals initiated a communication session with the base station, and on the downlink the order might be based on the amount of data to be transmitted to the various mobile terminals.

On the uplink cell 210<sub>5</sub>-DM<sub>S</sub> operates as described above with reference to the uplink shown in Figure 6, and on the downlink cell 110<sub>5</sub>-DM<sub>S</sub> operates as described above with reference to the downlink shown in Figure 7.

Figures 6, 7, and 8 illustrate how the order can be imposed on each cell independently of the order imposed in other cells. When the

order is imposed independently on each cell, then the order in each cell can be the same or different from each other. Furthermore, the order can be imposed on both links in some cells, only one link in other cells, and not imposed at all in yet other cells.

- 5 Alternatively, and advantageously, the order can be imposed on a portion, or all, or wireless communication system 100. Using the order in the multi-cell context provides the advantage of an even larger throughput improvement than the one cell context.

10 Figure 9 illustrates in more detail multi-cell portion 910-DM<sub>SP</sub> of wireless communication system 100 when the order is imposed on the mobile terminals in the entire portion and dirty paper coding is used on the downlink and multi-user detection is used on the uplink. Multi-cell portion 910-DM<sub>SP</sub> includes cells 210<sub>5</sub>-DM<sub>SP</sub>, 210<sub>8</sub>-DM<sub>SP</sub>, and 210<sub>9</sub>-DM<sub>SP</sub>, with DM<sub>SP</sub> used throughout the description and figures to represent that in a portion of a wireless communication system dirty-paper coding with order is used on the downlink, and multi-user detection with order is used on the uplink.

15 Similarly to cell 210<sub>5</sub>-DM<sub>S</sub> (shown in Figure 8), cell 210<sub>5</sub>-MD<sub>SP</sub> includes base station 215<sub>5</sub>-MD<sub>SP</sub> and mobile terminals 220<sub>51</sub>-MD, 220<sub>52</sub>-MD, and 220<sub>56</sub>-MD. Cell 210<sub>8</sub>-MD<sub>SP</sub> includes base station 215<sub>8</sub>-MD<sub>SP</sub> and mobile terminal 220<sub>83</sub>-MD. Cell 210<sub>9</sub>-MD<sub>SP</sub> includes base station 215<sub>9</sub>-MD<sub>SP</sub> and mobile terminals 220<sub>94</sub>-MD, and 220<sub>95</sub>-MD. Each of the base stations and mobile terminals can have one or more than one antennas. Conditions permitting, all of the base stations

20 215<sub>5</sub>-DM<sub>SP</sub>, 215<sub>8</sub>-DM<sub>SP</sub>, and 215<sub>9</sub>-DM<sub>SP</sub> communicate with all of the mobile terminals 220<sub>51</sub>-MD, 220<sub>52</sub>-DM, 220<sub>56</sub>-DM, 220<sub>83</sub>-DM, 220<sub>94</sub>-DM, and 220<sub>95</sub>-MD. There is an uplink signal between each antenna of each of the mobile terminals and each antenna of each of the base

stations; and there is a downlink signal between each antenna of each of the base stations and each antenna of each of the mobile terminals.

Base stations 215<sub>5</sub>-DM<sub>SP</sub>, 215<sub>8</sub>-DM<sub>SP</sub>, and 215<sub>9</sub>-DM<sub>SP</sub>, also communicate with MSC 960. In one embodiment of the invention, MSC 960 determines the selected downlink order—the order used on the downlink—and the selected uplink order—the order used on the uplink. On the downlink MSC 960 processes the signals to be transmitted in accordance with the selected downlink order using dirty paper coding. On the uplink MSC 960 decodes the received signals in accordance with the selected uplink order using multi-user detection. In other embodiments of the invention the order (the selected uplink order or the selected downlink order, or both) can be determined at any processor, controller, or other equipment within the wireless communication system, including one of the base station processors, such as for example, 560<sub>5</sub>-DM<sub>SP</sub>. On the downlink, the equipment that determines the order will either process the signals to be transmitted in accordance with the order, or will pass the order to other equipment that will process the signals. Preferably the equipment that process the signals to be transmitted has access to the signals to be transmitted to all of the mobile terminals in the plurality of mobile terminals on which a particular order is imposed. Similarly, on the uplink, the equipment that determines the order will either decode the received signal in accordance with the order, or will pass the order to other equipment that will decode the received signal.

The order can be determined as described above. In the illustrative embodiment, for example, the order on both the uplink and downlink is based on the order in which mobile terminals initiated a communication session with the base stations. (Although, as described above, the selected downlink order can be based on different



criteria than the selected uplink order.) Note that as described above, the signals from the same mobile terminal, even when there are several signals from the same mobile terminal to several base stations, count as only one element in the scheme of the order, there can be  
 5 exceptions when the signal are carrying files that have different performance needs.

If mobile terminal 220<sub>51</sub>-DM initiated a communication session with the base stations first, mobile terminal 220<sub>52</sub>-DM second, mobile terminal 220<sub>83</sub>-DM third, mobile terminal 220<sub>94</sub>-DM fourth, mobile terminal 220<sub>95</sub>-DM fifth, and mobile terminal 220<sub>56</sub>-DM sixth, then this is the order of the mobile terminals. Thus, on the downlink MSC 960 uses the signals to mobile terminal 220<sub>56</sub>-DM in determining the signal to mobile terminal 220<sub>95</sub>-DM, and mobile terminal 220<sub>56</sub>-DM is a phantom to mobile terminal 220<sub>95</sub>-DM. Similarly, MSC 960 uses the  
 10 signals to mobile terminals 220<sub>95</sub>-DM 220<sub>56</sub>-DM to determine the signal to mobile terminal 220<sub>94</sub>-DM, and so mobile terminals 220<sub>95</sub>-DM and 220<sub>56</sub>-DM are phantoms to mobile terminal 220<sub>94</sub>-DM. This process continues until MSC 960 uses the signals to mobile terminals 220<sub>52</sub>-DM, 220<sub>83</sub>-DM, 220<sub>94</sub>-DM, 220<sub>95</sub>-DM and 220<sub>56</sub>-DM in  
 15 determining the signal to mobile terminal 220<sub>51</sub>-DM, and so mobile terminals 220<sub>52</sub>-DM, 220<sub>83</sub>-DM, 220<sub>94</sub>-DM, 220<sub>95</sub>-DM and 220<sub>56</sub>-DM are phantoms mobile terminal 220<sub>51</sub>-DM.  
 20

Similarly on the uplink, MSC 960 decodes the uplink the signals mobile terminal 220<sub>56</sub>-DM to all of the base stations first. MSC 960  
 25 then decodes the uplink signals from mobile terminal 220<sub>95</sub>-DM to all of the base stations second, from mobile terminal 220<sub>94</sub>-DM third, from 220<sub>83</sub>-DM fourth, from 220<sub>52</sub>-DM fifth, and from 220<sub>51</sub>-DM sixth.

Figure 10 illustrates, for the portion of the system shown in Figure 9, which mobile terminals' signals are taken account of in

compensating for interference in which other terminals' signals, thus illustrating which mobile terminals are phantoms to which other mobile terminals.

Because mobile terminals 220<sub>52</sub>-DM, 220<sub>83</sub>-DM, 220<sub>94</sub>-DM, 220<sub>95</sub>-DM and 220<sub>56</sub>-DM are phantoms to mobile terminal 220<sub>51</sub>, the signal to mobile terminal 220<sub>51</sub> can be assigned a data rate and a power level based on its requirements without consideration of the signal to mobile terminals 220<sub>52</sub>-DM, 220<sub>83</sub>-DM, 220<sub>94</sub>-DM, 220<sub>95</sub>-DM and 220<sub>56</sub>-DM and without consideration of the highest obtainable system throughput. As described above, if mobile terminal 220<sub>51</sub> is constrained to a certain power level or requires a certain data rate, then mobile terminal 220<sub>51</sub>'s other criteria can be determined using the consideration that the signals to mobile terminal 220<sub>51</sub> are not interfered with by the signals to mobile terminals 220<sub>52</sub>-DM, 220<sub>83</sub>-DM, 220<sub>94</sub>-DM, 220<sub>95</sub>-DM and 220<sub>56</sub>-DM.

Similarly because mobile terminals 220<sub>83</sub>-DM, 220<sub>94</sub>-DM, 220<sub>95</sub>-DM and 220<sub>56</sub>-DM are phantoms to mobile terminal 220<sub>52</sub>, mobile terminal 220<sub>52</sub> can be assigned a data rate and a power level based on its requirements without consideration of the signal to mobile terminals 220<sub>83</sub>-DM, 220<sub>94</sub>-DM, 220<sub>95</sub>-DM and 220<sub>56</sub>-DM and without consideration of the highest obtainable system throughput.

Thus, the data rate and/or power level is assigned to the mobile terminals without determining the maximal system throughput, and without determining the maximal the weighted system throughput. Additionally, the data rate and/or power level are assigned such that the data rates of the terminals having a lower index in the order will not be decreased due to the presence of the terminals having a higher index in the order, and power levels of the terminals having a lower

index in the order will not be increased due to the presence of the terminals having a higher index in the order.

Figure 9 illustrates an embodiment of the invention where order can be imposed on both the downlink and the uplink in a portion of a wireless communication system when dirty paper coding is used on the downlink and multi-user detection is used on the uplink. In alternative embodiments of the invention order can be used to impose the order in which signals are taken into account in any compensation scheme that uses techniques that compensate for interference among signals within the system. For example, the order can be imposed on the downlink and/or the uplink when multi-user detection is used on both the downlink and the uplink. Similarly, the order can be imposed on the downlink and/or the uplink if dirty paper coding can be used on both the downlink and the uplink.

As can be seen from Figures 8 and 9 and the related descriptions, once it is known which mobile terminals are included in a particular order—an order used for a particular set of mobile terminals—and the order is imposed, the signals to and/or from the mobile terminals are processed in a similar manner regardless of whether the mobile terminals are communicating with one base station having many antennas or with many base stations having one or many antenna. Thus, the multi-cell portion can be viewed as one unit.

The multi-cell portion can include some of the cells of a wireless communication system as shown in Figure 9, or the multi-cell portion can include all of the cells in a wireless communication as shown in Figure 11. Figure 11 illustrates wireless communication system 900 where order is imposed on the mobile terminals in the entire wireless communication system pursuant to the principles of the invention, and

dirty-paper coding is used on the downlink and multi-user detection is used on the uplink in accordance with an embodiment of the invention. As described above, order can be used to impose the order in which signals are taken into account in any compensation scheme that uses techniques that compensate for interference among signals within the system, regardless of whether the same or different compensation schemes are used on the uplink or downlink.

Preferably, for both the uplink and the downlink, the transmitter requires (must know) the channel characteristics of the channel over which it is about to transmit the signals. Knowing the channel allows transmission using the concept of so-called virtual antennas. The concept of virtual antennas allows the signals to and/or from multiple transmit and/or receive antennas between the same mobile terminal and base station not to interfere with each other. For more information on virtual antennas (eigenmodes) see, for example, the R.R. Farrokhi, G.J. Foschini, R.A. Valenzuela "Link-Optimal Space-Time Processing with Multiple Transmit and Receive Antennas" reference.

The foregoing is merely illustrative and various alternatives will now be discussed. For example, in the illustrative embodiments the order is descending, that is the signal with the order of one suffers the least number of interferers, namely none. In alternative embodiments of the invention, the order can be ascending, that is, the signals with the order one suffer the most number of interferers. In this case, the signals are processed from the mobile terminal with last index order to the mobile terminal with the order of one. (For example, when multi-user detection is used, the signal from the mobile terminal with the last index order will be decoded first; and when dirty paper coding is used, the signal with the last index order is processed first.)

Although fifteen cells are shown in the illustrative embodiment, wireless communication system can contain any number of cells. One skilled in the art will appreciate that the wireless communication system can include significantly more than fifteen cells, which can extend outward from the illustrated fifteen cell. Alternatively, the wireless communication system can include fewer than fifteen cells.

In the illustrative embodiments the same compensation scheme is used on the downlink for all of the mobile terminals. In alternative embodiments of the invention, one compensation scheme can be used for some of the mobile terminals and another compensation scheme can be used for other mobile terminals. In this case, one selected downlink order is imposed on the first group of terminal, and a different order is imposed on a different group of terminal. For example, dirty paper coding can be used for most of the mobile terminals and multi-user detection can be used for other mobile terminals. Using multi-user detection for some mobile terminals may be beneficial when multi-user detection provides as good interference compensation as dirty paper coding for the particular mobile terminals. Similarly for the uplink one compensation scheme can be used for some of the mobile terminals and another compensation scheme can be used for other mobile terminals.

In the illustrative embodiments the same order is imposed on the same link (uplink or downlink) for all of the mobile terminals that are physically in a certain portion (whether one cell or multi-cell portion) of a wireless communication system. In alternative embodiments of the invention, a first order can be imposed on a first plurality of mobile terminals and a second order can be imposed on a second plurality of terminals, were both pluralities of mobile terminals are in the same portion of the wireless communication system. The first and second

orders can be based on the same or on different based on different criteria. A particular mobile terminal can belong to the first plurality at a first time and to the second plurality in a second time, regardless of whether the particular mobile terminal changed locations.

5       Order can be used in a one cell or multi-cell portion of a wireless communication system where the mobile terminals, the base stations or both, can have either one or multiple transmit and/or receive antennas. Furthermore, the number of transmit and/or receive antennas can vary from mobile terminal to mobile terminals and/or  
10       from base station to base station.

11       In the illustrative embodiment the antennas shown are both  
12       transmit and receive antennas, and equipment in the receiver  
13       separates received signals from the transmitted signals. In alternative  
14       embodiments, the receive and transmit antennas can be separate  
15       antennas. The number of receive and transmit at a particular mobile  
16       terminals and/or base station can be equal to each other or different  
17       from each other.

18       Additional compensation techniques can be used on the uplink,  
19       the downlink, or both to further improve the throughput. For example,  
20       the well-known techniques of time-sharing can be used in conjunction  
21       with dirty paper coding and/or multi-user detection. In this case,  
22       time-sharing can be used, for example, to have the signals between a  
23       particular mobile terminal and base station transmitted at certain  
24       rates at one time and at different rates at another time.

25       Additionally, one skilled in the art will recognize that although in  
26       the illustrative embodiment each cell is an omni sector, the cell can be  
27       divided into a plurality of sectors, with each sector having its own  
28       antennas.

Furthermore, although the terminals are illustrated as mobile telephones, the mobile terminals can be any terminals capable of wireless communication, such as, for example, fixed telephones, or computers.

- 5        Thus, while the invention has been described with reference to a preferred embodiment, it will be understood by those skilled in the art having reference to the specification and drawings that various modifications and alternatives are possible therein without departing from the spirit and scope of the invention.

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